

# Generalized Neutrino Isocurvature

Wolfram Ratzinger

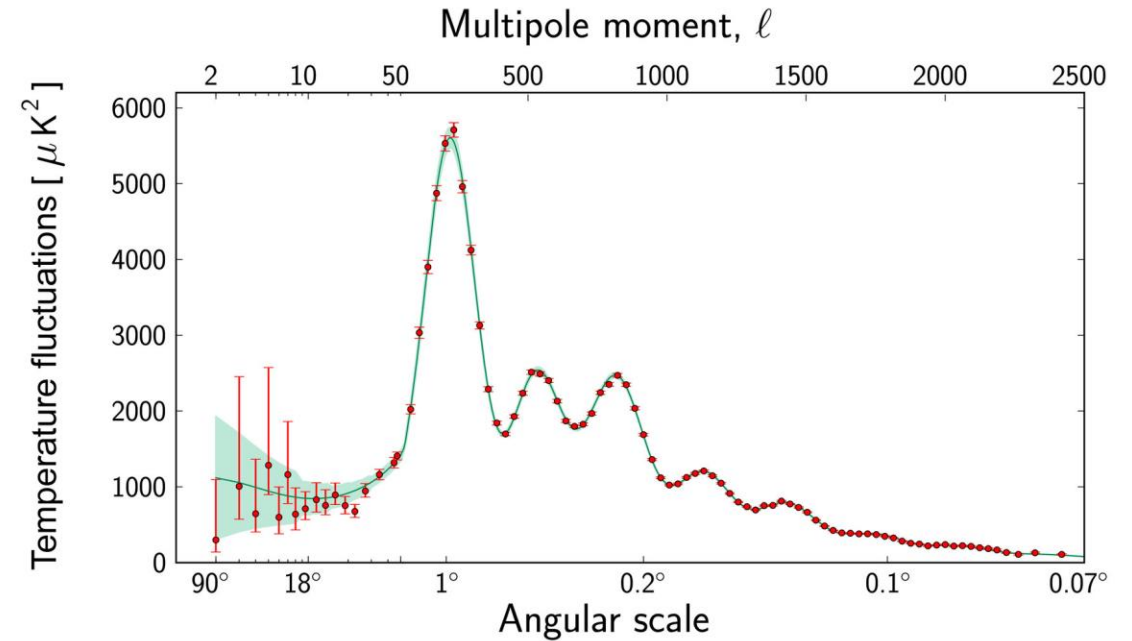
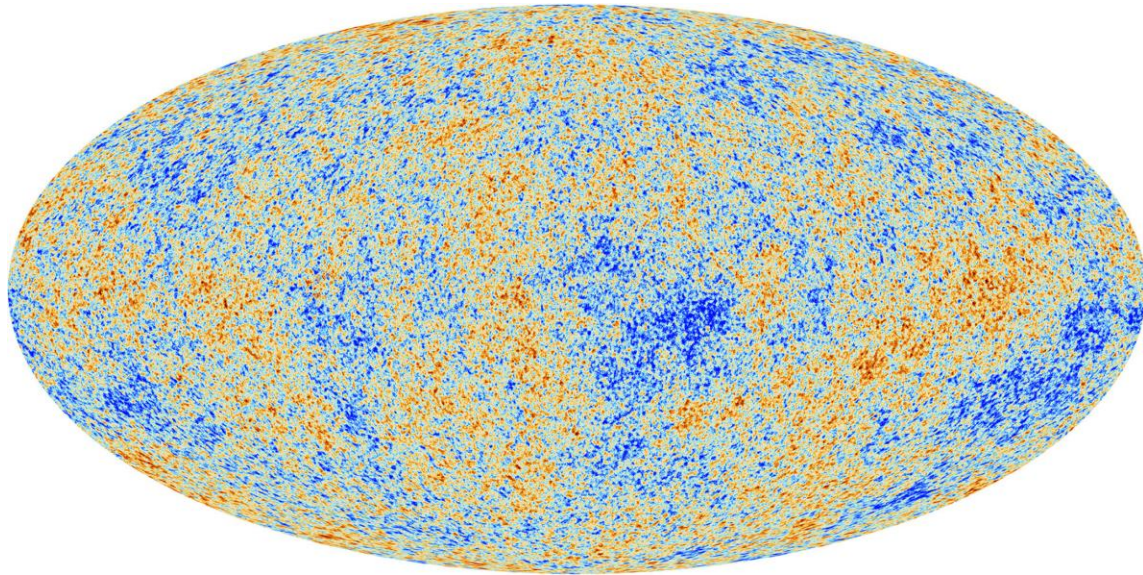
With Christopher Gerlach and Pedro Schwaller

Based on [2504.17047](#) and to appear



# The CMB so far:

- Adiabatic/curvature perturbations
  - Strict relation between overdensities in different fluids



# Search for isocurvature

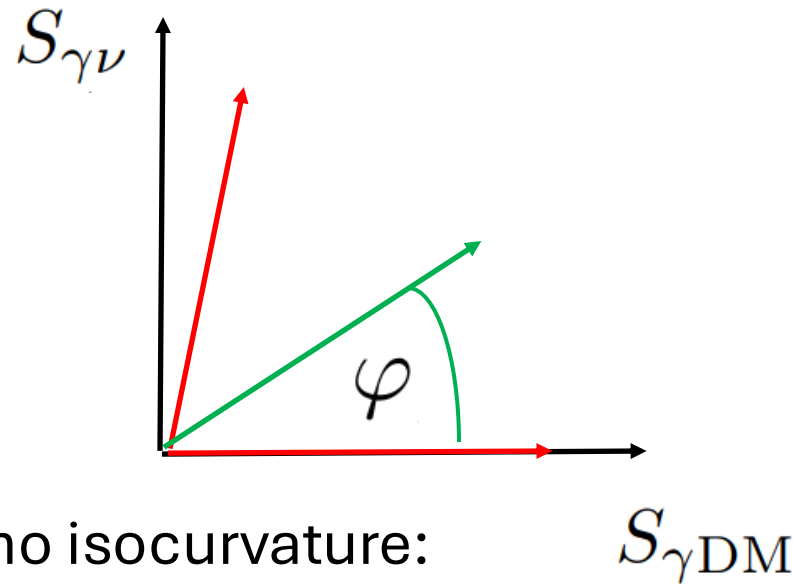
- Additional initial condition, with constant total density
- 2 (3) combinations:
  - Relative to photons DM, neutrino or baryon overdense  $S_{\gamma\text{DM}}$ ,  $S_{\gamma\nu}$ ,  $S_{\gamma\text{b}}$
- Need to generalize curvature power spectrum to 3x3 matrix

$$\langle \zeta \zeta \rangle \rightarrow \left\langle \begin{array}{ccc} \zeta \zeta & \zeta S_{\gamma\text{DM}} & \zeta S_{\gamma\nu} \\ \zeta S_{\gamma\text{DM}} & S_{\gamma\text{DM}} S_{\gamma\text{DM}} & S_{\gamma\text{DM}} S_{\gamma\nu} \\ \zeta S_{\gamma\nu} & S_{\gamma\text{DM}} S_{\gamma\nu} & S_{\gamma\nu} S_{\gamma\nu} \end{array} \right\rangle$$

- Very difficult to fit, no one has done it

# Search for isocurvature

- Instead pick one additional combination



Generalized neutrino isocurvature:  
-consider all ratios out of neutrino  
and DM isocurvature

So far people considered:  
-one "random" combination  
-DM isocurvature only

# Outline

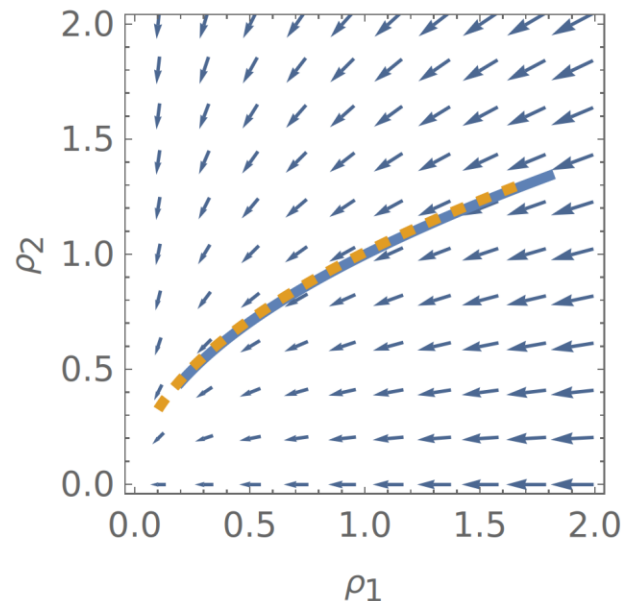
I Part: Neutrino isocurvature comes generically with DM isocurvature

II Part: CMB observables with general isocurvature

# Adiabatic vs. Isocurvature perturbation

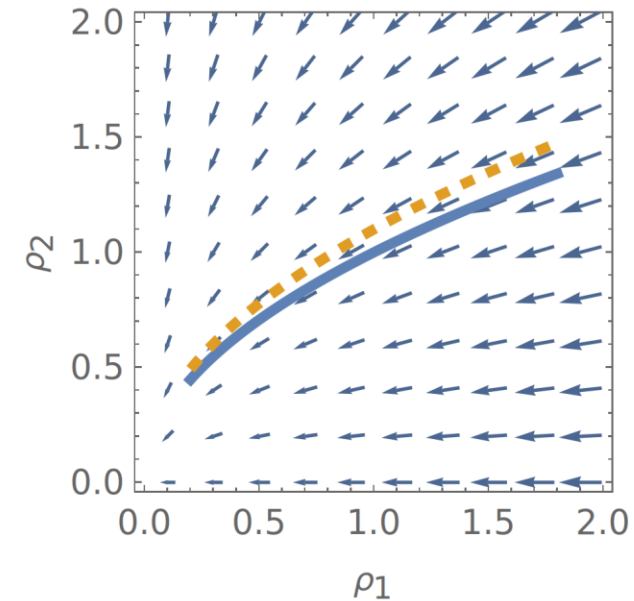
Wands, Malik, Lyth, Liddle 2000

- Perturbation on super-horizon scale correspond to patches perturbed relative to background evolution



perturbed patch  
background

Adiabatic: Perturbed patch only  
ahead of background



Isocurvature: Perturbed patch goes  
through different history

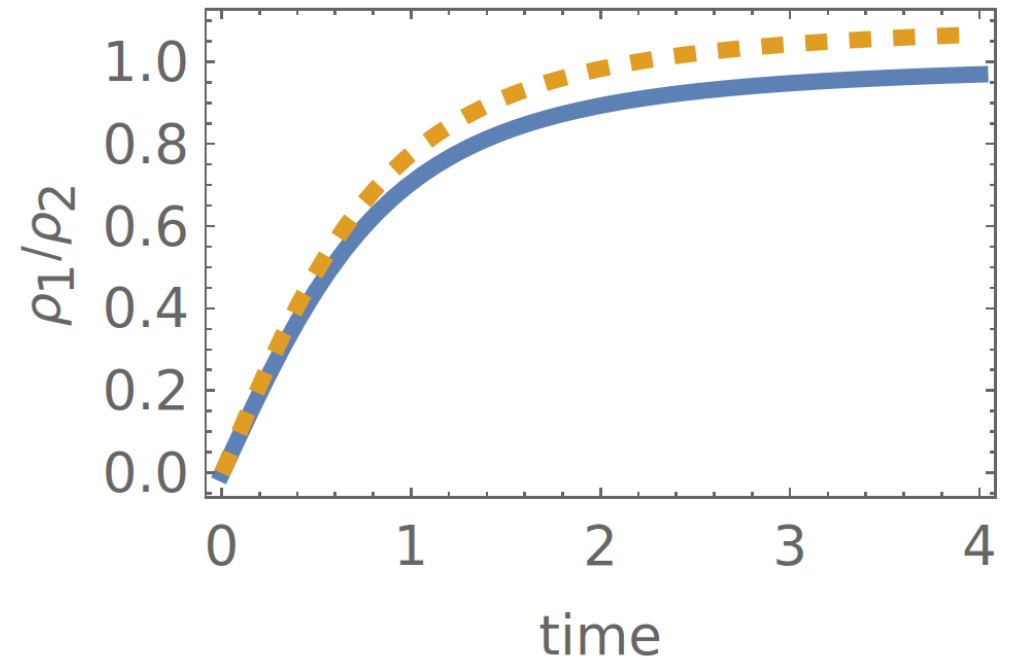
# Isocurvature: Special case

- Consider conserved number densities
- If  $\rho_i$  is conserved number density

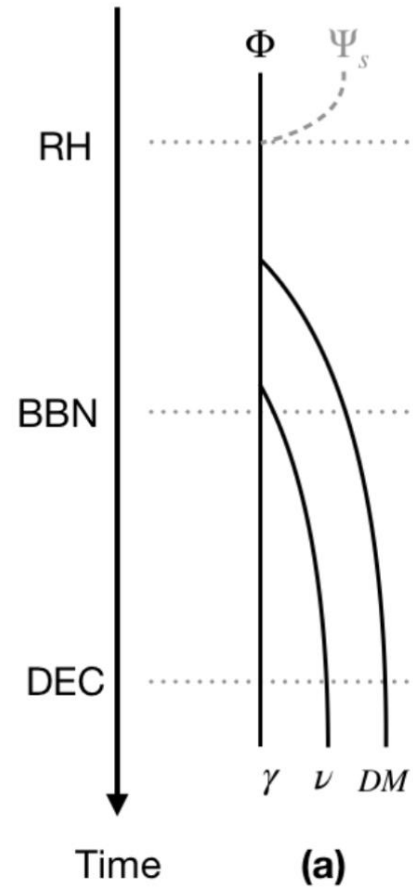
$$\dot{\rho}_i = -3H\rho_i$$

may define isocurvature as

$$S_{ij} = \delta \left( \frac{\rho_i}{\rho_j} \right) / \frac{\rho_i}{\rho_j}$$



# Cosmological histories

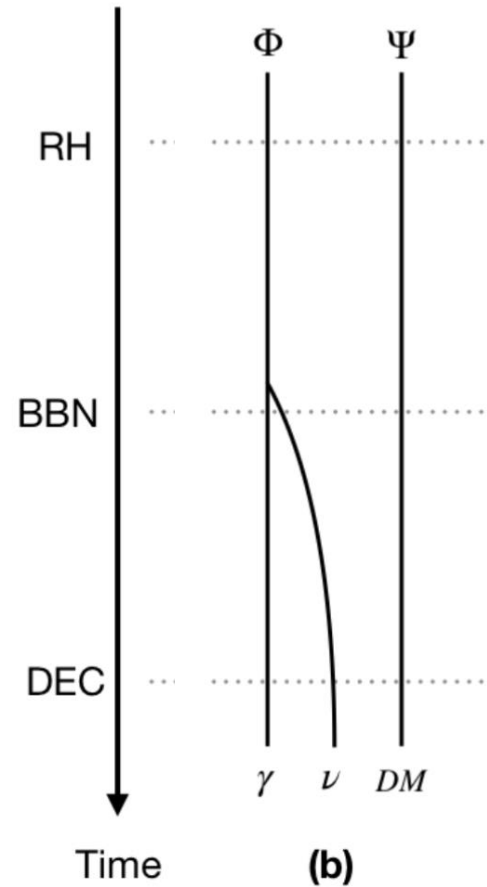


Only adiabatic perturbation

Weinberg 2004



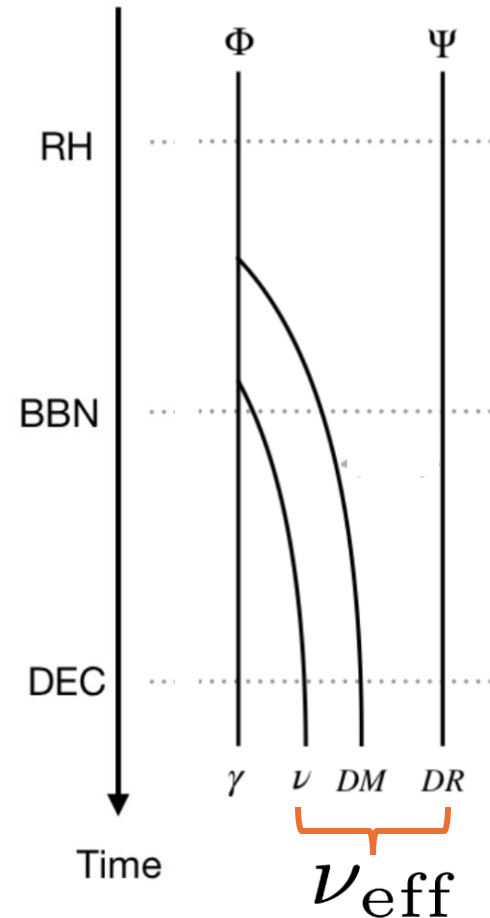
# Cosmological histories



e.g. ultra light DM from  
misalignment mechanism

Curvature + DM Isocurvature

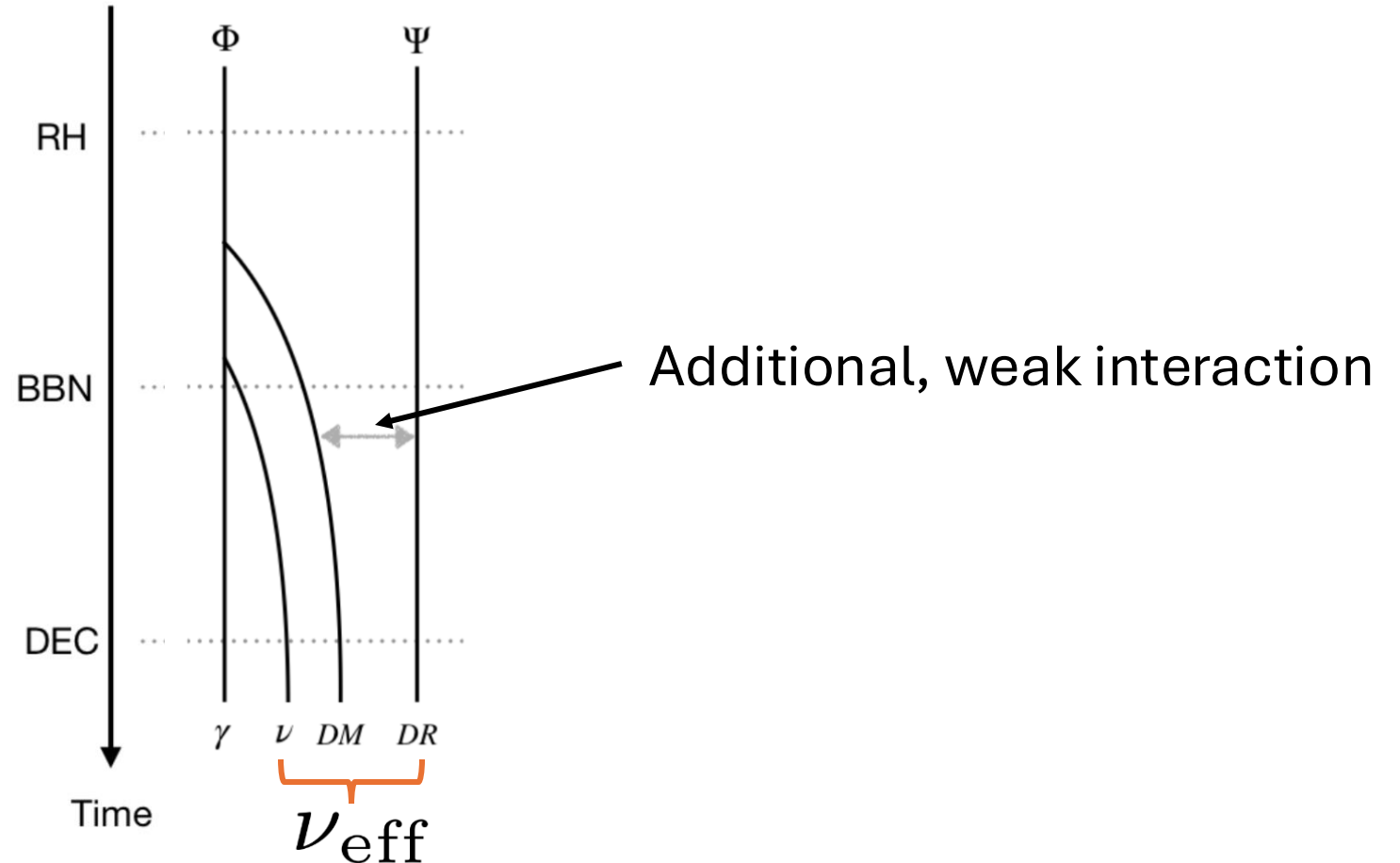
# Cosmological histories



Neutrinos are just free-streaming dark radiation for CMB

Curvature + neutrino Isocurvature  
-> naively no DM Isocurvature

# Cosmological histories

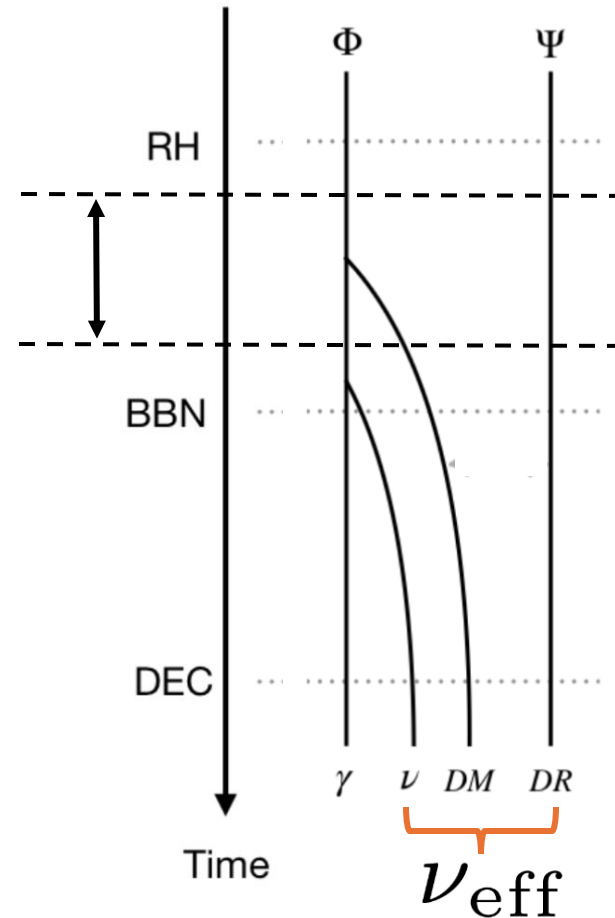


Curvature + neutrino Isocurvature  
Also generates DM Isocurvature

# Cosmological histories

Only consider this period

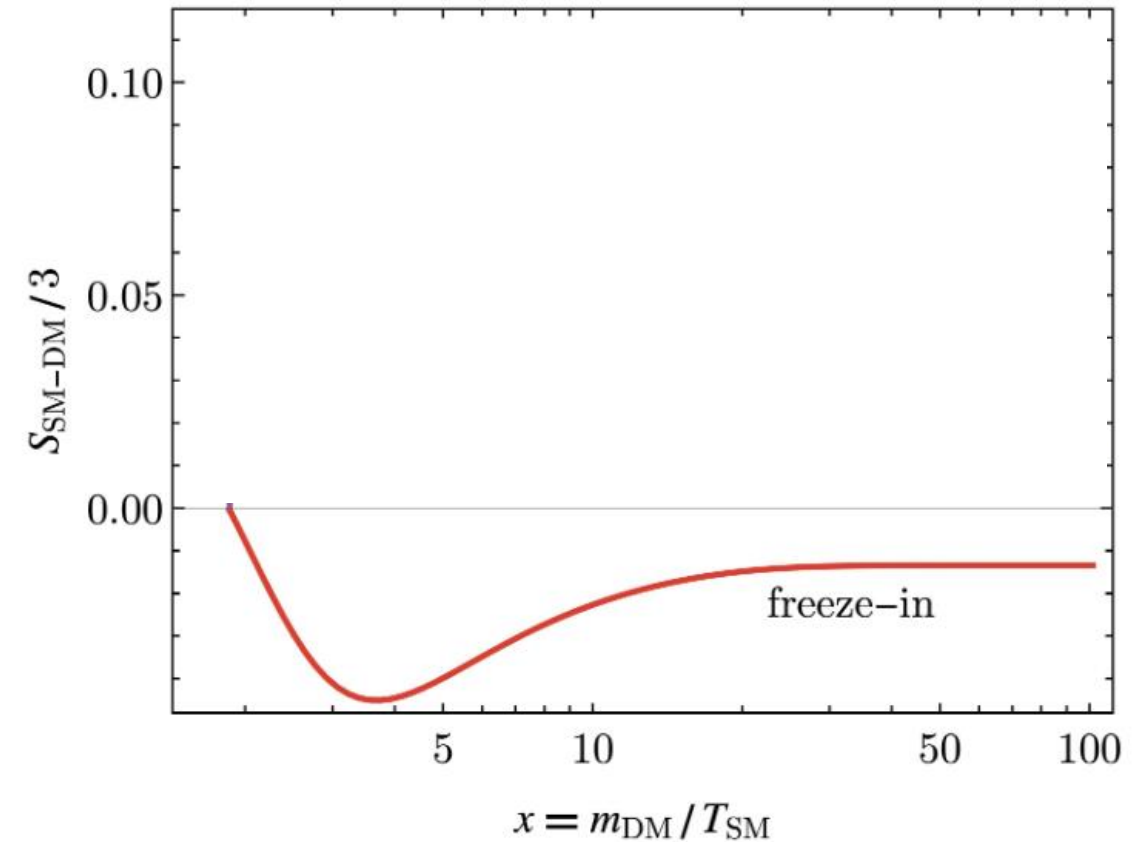
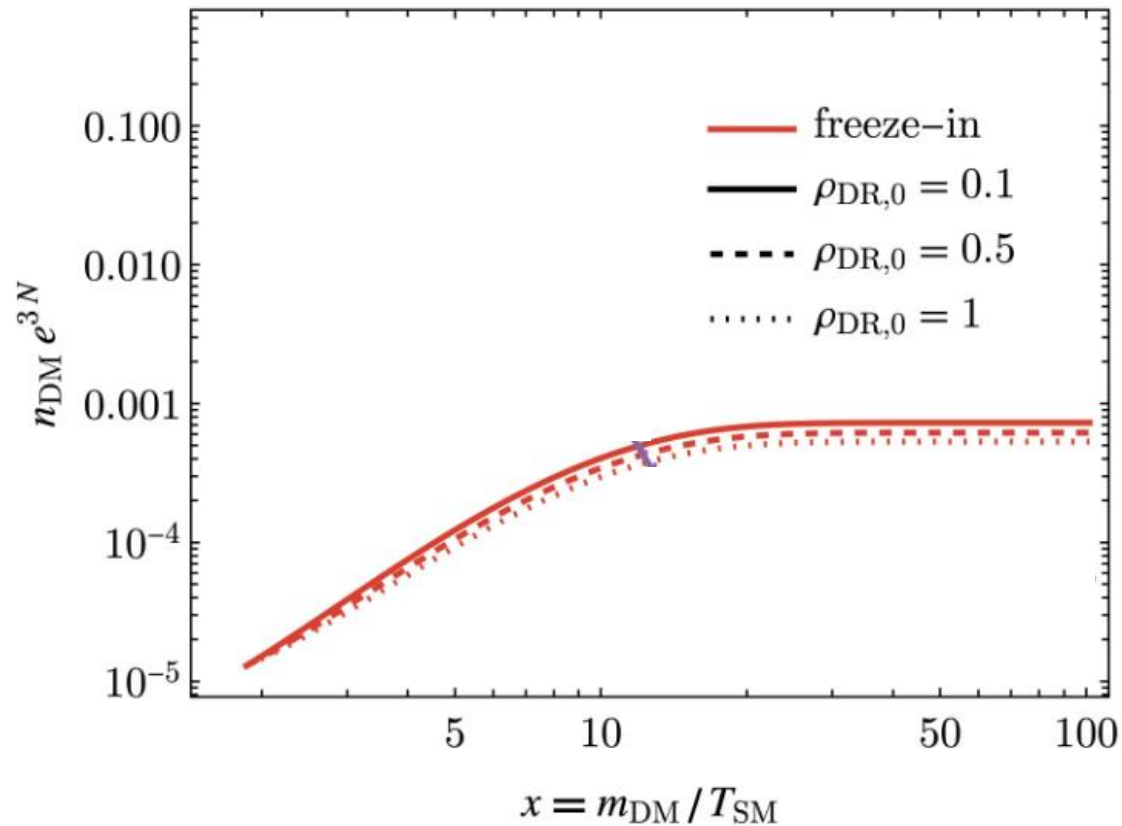
- freeze-in
- freeze-out
- ...



Curvature + neutrino Isocurvature  
-> gravitationally induce DM Isocurvature

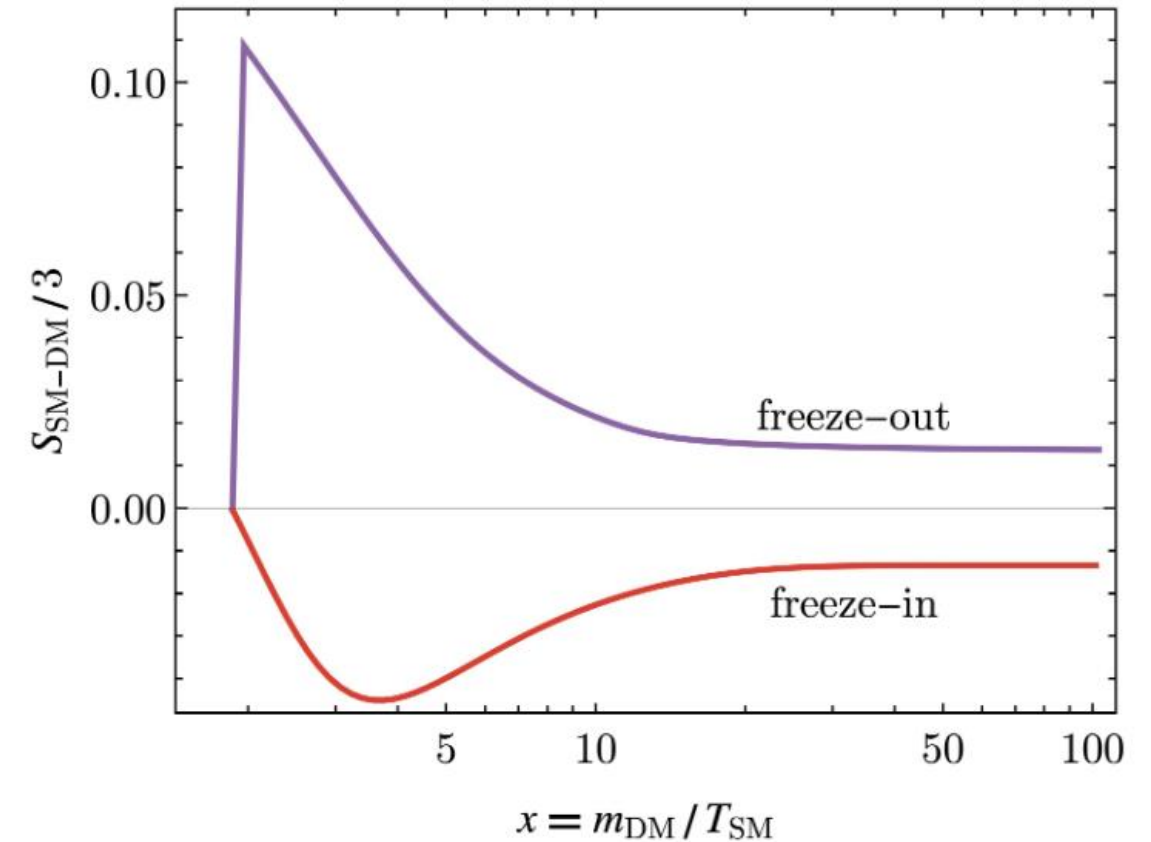
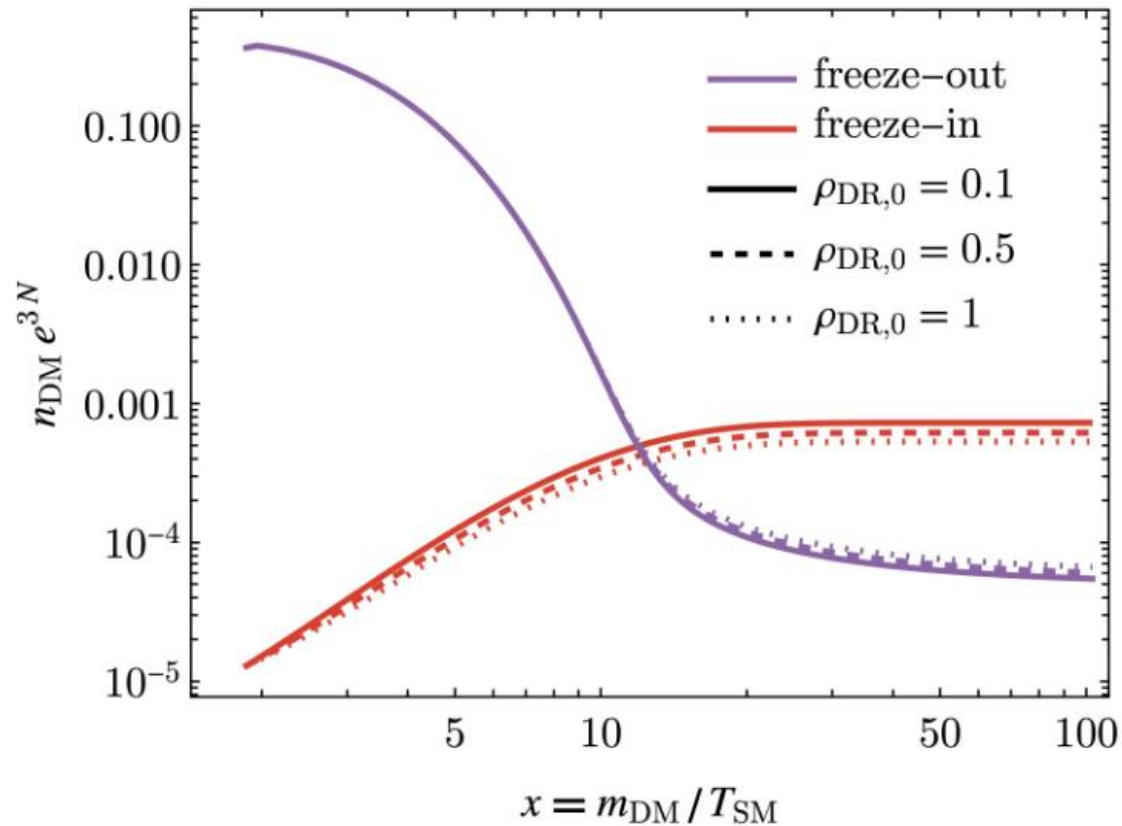
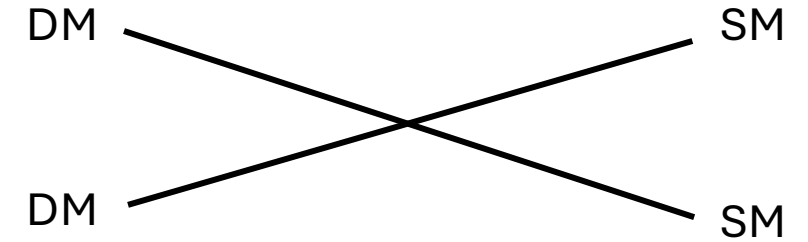
# Freeze-in

Yield  $Y = \frac{n_{\text{DM}}}{n_{\text{SM}}} \sim \frac{\Gamma(T_{\text{SM}} = m)}{H(T_{\text{SM}} = m)}$



# Freeze-out

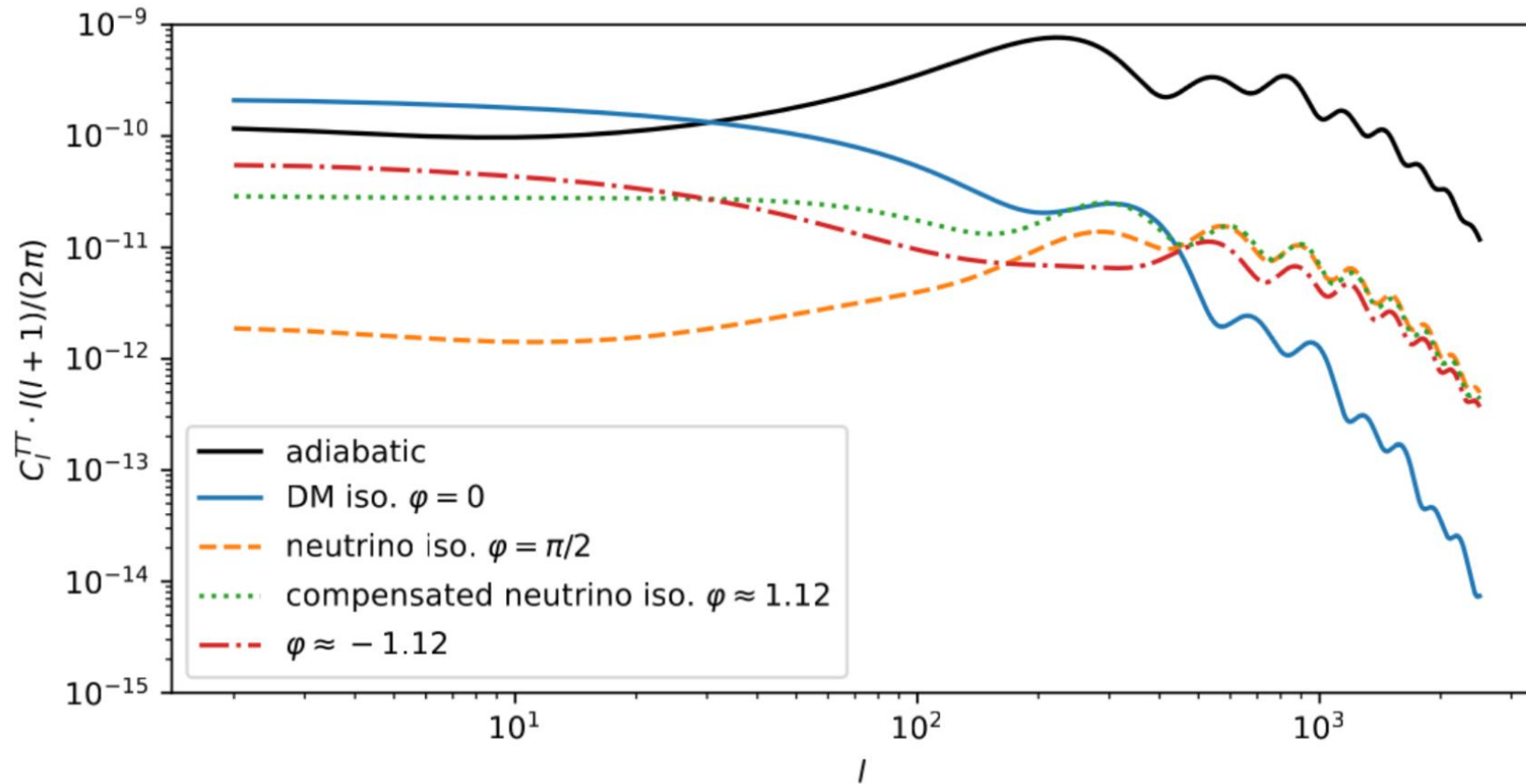
Yield  $Y \sim Y_{\text{eq}}(T^*), \Gamma_{\text{an}}(T^*) = H(T^*)$



# II Part: CMB observables

# The CMB spectrum

Observables depend on  $\tan(\varphi) = \frac{S_{\gamma\nu}}{S_{\gamma\text{DM}}}$



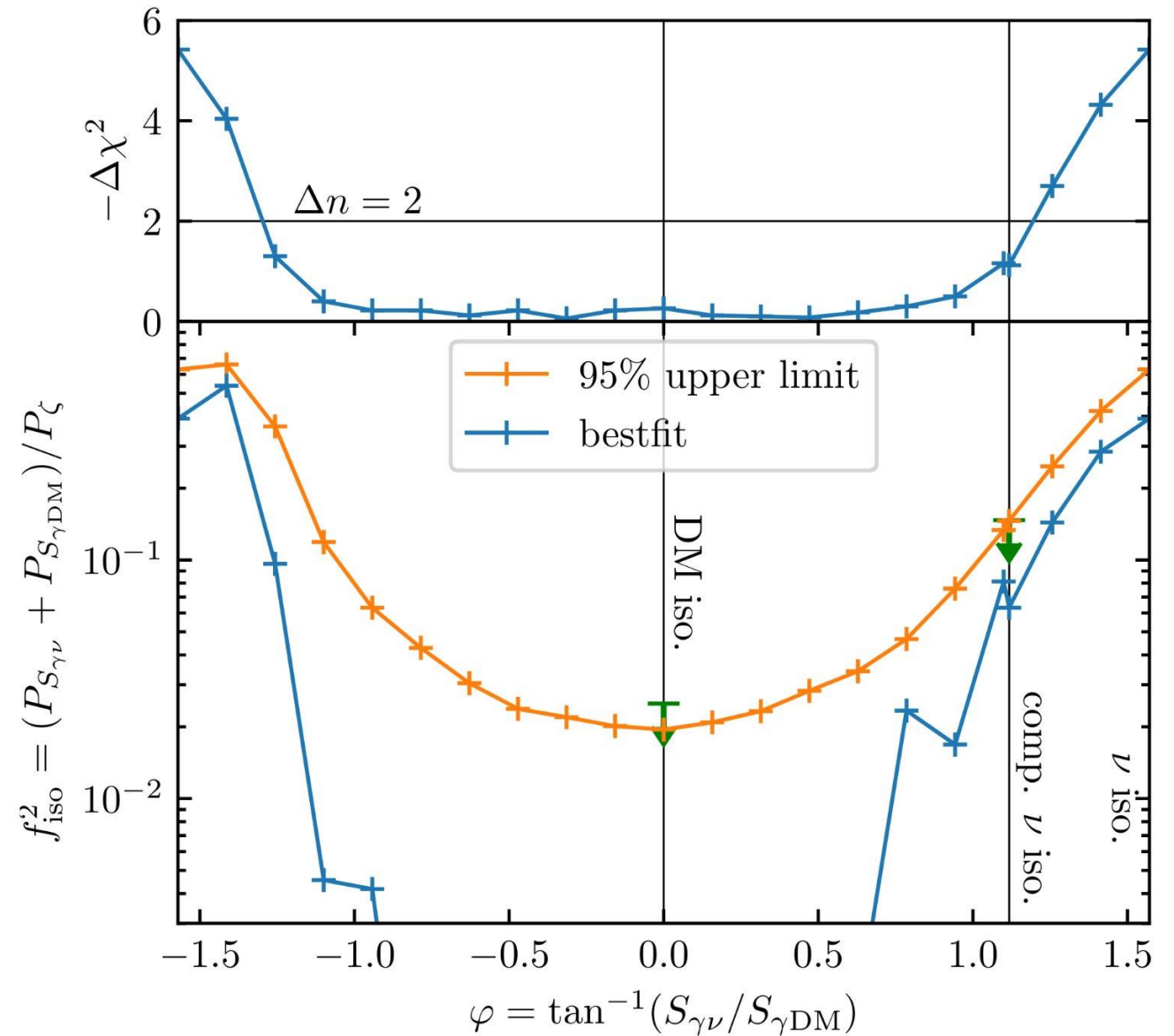


# Result of CMB and LSS fit

-Fit to Planck and BAO data

-Varying isocurvature amplitude and correlation

-Fixed spectral index  
 $n_{\text{iso}} = 1$



# Future searches

Staying optimistic:

Let's assume CMB  
stage 4 finds  
isocurvature here

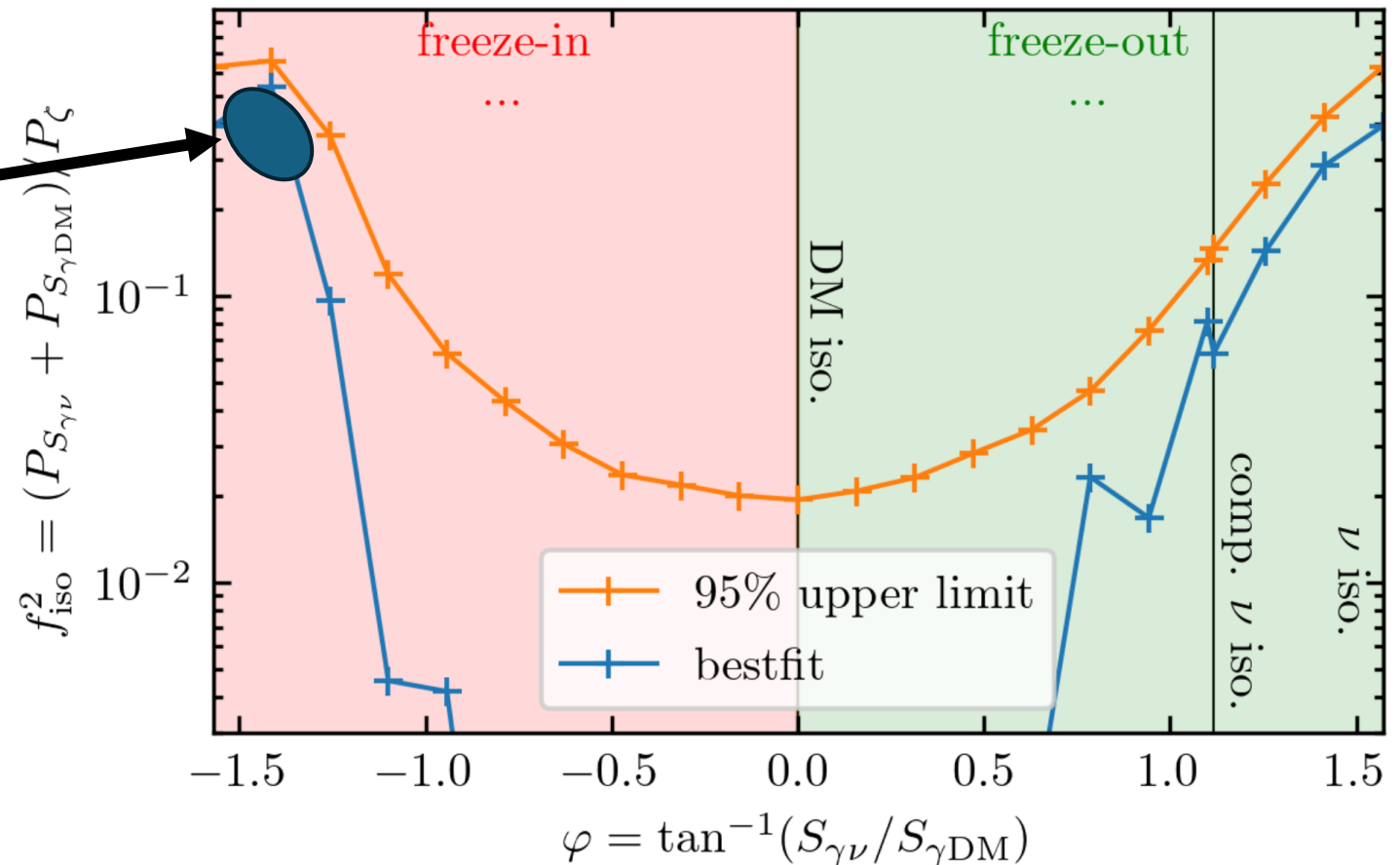
-> DM is produced via  
freeze-in

Requires assumptions:

-> No direct interaction

-> baryogenesis  
unaffected

->...



# Cosmological archaeology



A few more hints...



$$\frac{S_{\gamma\nu}}{S_{\gamma\text{DM}}}$$



Full cosmological history

# Conclusion

- Cosmologies with neutrino isocurvature generically feature fully correlated DM isocurvature
  - > Should included general case in searches
- If detected, this provides valuable information about the entire history

Thanks